

# Mark Scheme (Results)

Summer 2016

Pearson Edexcel GCE Decision Mathematics 2

6690/01

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### **EDEXCEL GCE MATHEMATICS**

#### **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for `knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- ☐ The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.

- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

Question Number	Scheme	Mark	s
<b>1.</b> (a)	e.g. in the practical problem each vertex must be visited at least once. In the classical problem each vertex must be visited just once	B2, 1, 0	(2)
	A - D - C - F - B - E - G - A 12+16+19+25+14+41+22 = 149	M1	
(b)	A - D - C - F - G - E - B - A	A1	
	12+16+19+25+41+14+31 = 158	A1	(3)
(c)	RMST weight = 86 (miles)	B1	
	86 + 12 + 15 = 113 (miles)	M1 A1	(3)
(4)	112 < antimal distance < 140	B2, 1, 0	(2)
( <b>d</b> )	$113 \leq \text{optimal distance} \leq 149$	10 marks	S

Notes for Question 1

a1B1: Understands the difference is connected to the number of times each vertex may be visited (but maybe incorrectly attributed). Must be an attempt at a difference (so must refer to both the classical and practical problems explicitly). Technical language (vertex/node) must be correct. Need not imply each/every/all (oe) vertices for this first mark

a2B1: Correctly identifies which is classical and which is practical and correctly states the difference. Must imply that each/every/all (oe) vertices are visited, so for example, 'the practical problem visits a vertex at least once while the classical visits a vertex only once' is B1B0 (note that B0B1 is not possible in (a))

b1M1: Either one correct route, must return to A, or one correct length stated (do not isw in part (b) if correct lengths seen but are then doubled)

b1A1: One correct route, must return to A and corresponding length correct

b2A1: Both routes correct and their corresponding lengths correct

c1B1: CAO for RMST weight (either 86 or 20 + 16 + 14 + 19 + 17) – maybe implied by later working c1M1: Adding 12 + 15 (the two least weighted arcs) to their RMST length (the length of their RMST must be in the interval  $66 \le RMST \le 106$ ) – this mark maybe implied by the correct value for the lower bound c1A1: CAO - if 113 seen without working then award all 3 marks in (c)

d1B1: Their numbers correctly used, accept any inequalities or any indication of interval from their 113 to their 149 (so 113 - 149 can score this mark). This mark is dependent on two totals seen in (b), however, neither of the two totals need to be correct. Please note that UB > LB for this mark d2B1: CAO (no follow through on their values) including correct inequalities or equivalent set notation (but

d2B1: CAO (no follow through on their values) including correct inequalities or equivalent set notation (but condone 113 <optimal distance  $\le 149$ )

Number 2. (a)	Scheme	Marks
	Saturated arcs: SB, SC, AE, DT, FT	M1 A1 (2
(b)	59	B1 (1
(c)	$C_1 = 72, C_2 = 86$	B1 B1 (2
(d)	SABCFET	B1 (1
(e)	The cut through DT, AE and CF (or DT, AE, BC and SC) has a value 62	M1
	Value of the flow is 62, so by max flow – min cut theorem, flow is maximal	A1 (2 8 marks
	Notes for Question 2	1
e1M1: Th check car e1A1: Mu	AO (72)	

Number	Scheme	Marks
<b>3.</b> (a)	Since maximising, subtract all elements from some value $\geq 72$	
	e.g $\begin{bmatrix} 11 & 22 & 25 & 49 \\ 1 & 10 & 52 & 11 \\ 2 & 23 & 24 & 23 \\ 0 & 4 & 5 & 5 \end{bmatrix}$	M1
	Reduce rows $\begin{bmatrix} 0 & 11 & 14 & 38 \\ 0 & 9 & 51 & 10 \\ 0 & 21 & 22 & 21 \\ 0 & 4 & 5 & 5 \end{bmatrix}$ and then columns $\begin{bmatrix} 0 & 7 & 9 & 33 \\ 0 & 5 & 46 & 5 \\ 0 & 17 & 17 & 16 \\ 0 & 0 & 0 & 0 \end{bmatrix}$	M1 A1
	$\begin{bmatrix} 0 & 2 & 4 & 28 \\ 0 & 0 & 41 & 0 \\ 0 & 12 & 12 & 11 \\ 5 & 0 & 0 & 0 \end{bmatrix} $ followed by $\begin{bmatrix} 0 & 0 & 2 & 26 \\ 2 & 0 & 41 & 0 \\ 0 & 10 & 10 & 9 \\ 7 & 0 & 0 & 0 \end{bmatrix}$	M1 A1ft M1 A1
	Optimal allocation is $F = 1$ , $A = 2$ , $Z = 3$ , $E = 4$	A1 (8)
(b)	(Total score is = ) 248	B1 (1)
	Notes for Question 3	9 marks
a1M1· Su		then adding a
value whi a2M1: Re maximum a1A1: CA a3M1: Dc a2A1ft: Fo a4M1: On lines need a3A1: CS	ibtracting from some value which must be $\geq 72$ or all values made negative and ich must be $\geq 72$ . Condone no more than two errors educing rows <b>and then</b> columns – candidates may combine the two stages of co in to a minimum problem and row reduction which is acceptable	nverting from a s to 3 lines needed
value whi a2M1: Re maximum a1A1: CA a3M1: Dc a2A1ft: Fo a4M1: On lines need a3A1: CS a4A1: CA	abtracting from some value which must be $\geq 72$ or all values made negative and ich must be $\geq 72$ . Condone no more than two errors educing rows <b>and then</b> columns – candidates may combine the two stages of co in to a minimum problem and row reduction which is acceptable AO puble covered +e; one uncovered –e; and one single covered unchanged. 2 lines follow through on their previous table – no errors ne double covered +e; one uncovered –e; and one single covered unchanged. 3 ded (so getting to the optimal table) SO on final table (so must have scored all previous marks) AO – this mark is dependent on all M marks being awarded	nverting from a s to 3 lines needed
value whi a2M1: Re maximum a1A1: CA a3M1: Do a2A1ft: Fo a4M1: On lines need a3A1: CS	ibtracting from some value which must be $\geq 72$ or all values made negative and ich must be $\geq 72$ . Condone no more than two errors educing rows <b>and then</b> columns – candidates may combine the two stages of co in to a minimum problem and row reduction which is acceptable AO puble covered +e; one uncovered –e; and one single covered unchanged. 2 lines follow through on their previous table – no errors ne double covered +e; one uncovered –e; and one single covered unchanged. 3 ded (so getting to the optimal table) SO on final table (so must have scored all previous marks) AO – this mark is dependent on all M marks being awarded	nverting from a s to 3 lines needed

Question Number						Sch	eme						Ν	Marks	5
<b>4.</b> (a)	e.g.var	iable <i>x</i>	c was in	creas	ed first.	since i	t has b	ecome a	basic	c varial	ole		B1		(1)
(u)	0.8	140101			<i>•••</i>			•••••	e usi						(-)
	b.v.	x	y	Z.	r	S	t	Value	ro	ow ops					
	z	0	2.5	1	0.5	-1.5	0	5		$\frac{R_1 \div 2}{R_1 \div 2}$			M1	A1	
	x	1	-5.5	0	-1.5	5.5	0	3		$\frac{R_1 + 2}{R_2 - 3R_1}$			M1		
<b>(b)</b>	t	0	3.5	0	0.5	2.5	1	8		$\frac{1}{R_3 + R_1}$					
	Р	0	13	0	2	-5	0	27		$R_4 + 4R_1$			A1ft	A1	(5)
					1			L	1						(5)
(c)	P+13	y+2r	-5s = 2	27									B1ft		(1)
( <b>d</b> )	P = 27	′−13y	-2r+3	5 <i>s</i> , sc	we car	increa	se the	profit by	incre	easing	s, hen	ice not	-	·	(2)
(4)	optima	1											9 ma	ırks	
4.5.4			6				r Que	estion 4							
a1B1: e.g.	. identifi	es x, r	eters to	basic	variab	le (oe)									
<b>TO I I</b>								-					<b>(-</b> ) <b>(</b> )		
If nivotin	ig on a n	legativ	ze valuo	e or o	n a val	ue fron	ג the ו	c or y col	umn	then r	io ma	irks in	(b), (c) (	or (d	)
n proun	0	8	e and												
-	0	C													
b1M1: Co	orrect piv	vot loc	ated (2	in co	lumn z)	-									
b1M1: Cc b1A1: Piv	orrect piv	vot loc correct	ated (2 includ	in co ing c	lumn z) <b>hange c</b>	of b.v. (	so the	r must b	e rep						
b1M1: Co b1A1: Piv b2M1: Al	orrect piv vot row c II values	vot loc correct in one	ated (2 <b>includ</b> of the	in co <b>ing c</b> l non-p	lumn <i>z</i> ) <b>hange c</b> pivot rov	of b.v. ( ws corre	so the ect <b>or</b>	<i>r</i> must b one of th	e rep e nor				ımns (y, i	r, s 01	r
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b1M1: Cc b1A1: Piv b2M1: AI value) cor b2A1ft: R value) cor b3A1: CA given in to c1B1ft: D P = 13y + d1B1: Mu 'negatives d2B1: CA	borrect pive vot row c ll values rrect foll Row oper rrect foll AO – no erms of c Dependen -2r - 5s ust have s in profit AO – dep	vot loc correct in one owing rations owing follow old row at on th + 27 is gained it row' enden	ated (2 includ of the throug used co throug w 1 - ig ne secon s incorr l both N with n t on the	in col ing cl non-p h thei orrect h thei h – al <b>nore</b> nd M ect) A mar o furt	lumn z) hange o pivot row r choice ly at lea ir choice ll values <b>b.v. co</b> l mark ea wark ea wark ea cks in (b	of b.v. ( ws correct of pive ast twice of pive and ro and ro urned in ) and m lanation at equation	so the ect or ot from e, i.e. + ot from w ope or this (b) - hust re- a given ion in	r must b one of th n columr two of th n columr rations co mark must be fer to ine	e rep e nor z e nor z orrect an eq	n zero-a n zero-a tly state quation <b>sing</b> y, a	and-or and-or ed – a conta r or s.	ne colu ne colu Illow if ining <i>I</i> Do no	imns (y, r Frow ope P (please it accept	r, s o ratio note	r ns that
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b1M1: Co b1A1: Piv b2M1: AI value) cor b2A1ft: R value) cor b3A1: CA given in to c1B1ft: D P = 13y + d1B1: Mu 'negatives d2B1: CA that could	principal prices of the price	vot loc correct in one owing rations owing follow old row old row old row t on the +27 is gained it row' enden eased a in the $\frac{1}{2}$	ated (2 <b>includ</b> of the throug used co throug $w \ 1 - ig$ he second s incorr l both M with n t on the and stat z colum	in co ing c non-p h thei orrect h thei h – al <b>more</b> nd M ect) A mar o furt correct es 'no in (ca	lumn z) hange o pivot row r choice ly at lea r choice ll values <b>b.v. co</b> l mark ea ks in (b her exp ect profit of optim n score y 11/3 2/3	of b.v. (i ws corrections corrections to be a correction of pive e of pive of	so the ect or ot from $b_{i}$ the form	r must b         one of th         n column         two of th         n column         rations compared         mark         must be         fer to ind         (c). Spec         of B1 M	e repi e nor z e nor z orrect an eq creas ifical $\overline{z}$ $\overline{z}$	n zero-a n zero-a tly stat quation sing $y$ , $t$ lly iden M1A1 $t$	and-or and-or ed – a conta r or s. atifies A0 B Va $-\frac{1}{2}$	ne colu ne colu illow if ining $h$ Do no s as th 1 B0B 1 1 B0B 1 1 1 1 1 1 1 1 1 1	imns (y, r Frow ope (please it accept e next va	r, s o eratio note uriabl	r ns that
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Question Number					Sche	me						Mark	.s
<b>5.</b> (a)	(total) supply	/ > (total) (	demand	l								B1	(1)
(b)		$     \frac{1}{2} \\     3 \\     4     Demand   $	A 18 22 24 21 40	B 23 17 21 22 20	C 20 25 19 17 25	) 5 9 7	Dumm 0 0 0 0 14	y	Supply 15 36 28 20			B1	(1)
(c)		1 2 3 4 Demand	A 15 25	5	B 11 9 20	C 19 6 25	D 14 14	,	pply 15 36 28 20			B1	(1)
	$     \begin{array}{ c c c c }                              $	$\begin{array}{c c} B \\ \hline 17 + \theta \\ 3 - \theta \end{array}$	C 25 1	D θ 4-θ	givii	ng _	1 2 3 4	A 15 16 9 Exit	B 20 ing cell	C 25 is B3	D 3 11	M1 A1	
( <b>d</b> )			Shadow costs 0 4 3 3	1 2 3 4	18 A X X 3 X	13 B 10 X 5 6	C 0 4 5 X	-3 D 3 -1 X X X				M1 A1	
				Ente	ring c	ell is	C4						
	A 1 2 3 4	B C 25- θ	-θ 3·	$\frac{D}{+\theta}$	Į	givin	g 1 3 4	9		C 14 11 ell is [	D 14 04	M1 A1	(6)

Question Number			Sche	me				Marks
(e)		adow osts         0         1           0         1         4         2           5         3         3         4	18 A X X 1 X	13 B 10 X 3 6	14 C 6 7 X X X	-5 D 5 1 X 2		M1 A1
Optin	nal since no nega	ative improve	ement i	ndices				A1 (3) 12 marks
			otes for					
a1B1: CAO (or t	o make demand :	= supply or b	because	demar	ıd ≠ su	ipply (o	e))	
b1B1: CAO								
c1B1: CAO								
d2A1: Shadow c d3M1: A valid ro		B(-5), C(-2), legative II ch	D(-21), losen, c	, 1(18), only on	e empty	square	used, $\theta$ 's l	
e1A1: CAO for t positive IIs	shadow costs an he shadow costs part e) + reason -	[Alt: A(0), H					-	found (4(21)] and the 9

Question Number	Ncheme										Marks
6. (a) Row mins $\{-3, 0, -4\}$ Column max $\{5, 5, 4\}$											M1
<b>6.</b> (a)	$\operatorname{Kow} \operatorname{Maximin} (0) \neq \operatorname{Column} \operatorname{Minimax} (4) (so not stable)$										
<b>(b)</b>	E.g. add	5 to eac	ch eleme	ent							B1
	Let $p_1, p_2$	$p_2, p_3$ be	e the pro	bability	of (A) p	laying 1	, 2 and 3	3 respec	tively		B1
	Let $p_1, p_2, p_3$ be the probability of (A) playing 1, 2 and 3 respectively (where $p_1, p_2, p_3 \ge 0$ )										
	Let V =		-	ne (to pl	ayer A)						<b>B</b> 1
	Maximis	se ( <i>P</i> =)	V								B1
	Subject	to:									
	V-10p		$-p_3 + r =$	= 0							
	$V-2p_1$	$-10p_{2}$ -	$-4p_3 + s$	= 0							M1 A1 A1
	$V-6p_1$	$-5p_2 - 9$	$9p_3 + t =$	:0							(7)
	$p_1 + p_2 - p_1 + p_2 - p_2 $	$+ p_3(+u)$	)=1								
	(r,s,t,u)	≥0)									
	e.g. (add	ling 5 to	each el	ement)							
	b.v.	V	$p_1$	$p_2$	$p_3$	r	S	t	и	Value	
		1	- <b>10</b>	- <b>7</b>	- <b>1</b>	1	0	0	0	0	B1 M1 A1
( <b>c</b> )	r s	1	-10	-10	-1 -4	0	1	0	0	0	(3)
	$\frac{3}{t}$	1	-2	-10		0	0	1	0	0	
	u u	0	1	1	1	0	0	0	1	1	
	P	-1	0	0	0	0	0	0	0	0	
			-		_		-	-			12 marks

a1M1: Finding row minimums and column maximums – condone one error

a1A1: CAO must state that  $0 \neq 4$  (oe) – if  $0 \neq 4$  stated with no working then award M1A0 only

b1B1: Making all terms non-negative (any addition  $\geq 4$  is acceptable)

b2B1: Defining probability variables

b3B1: Defining V

b4B1: 'maximise' + function/expression

b1M1: At least three (of the four) equations **or** inequalities in V,  $p_1$ ,  $p_2$ ,  $p_3$  (with all  $p_i$  terms in the first three constraint equations having correct signs for the coefficients) – condone no slack variables for this mark b1A1: CAO - the three constraints involving V and  $p_i$  expressed as equations with slack variables

b2A1: Probability sum equation correct (allow presence of a slack variable in this equation)

c1B1: All row and column labels correct for Simplex tableau

c1M1: Any two (numerical in nature) rows correct following from their constraints **or** a 'correct' answer (no follow through) with either one column or one row or one of both (so both a row and column) missing c1A1: CAO – candidates may not label columns or rows in the order as given above – please check these carefully. Furthermore, candidates may add any value  $\geq 4$  which will change the nine bolded values above (so if +4 has been used this will increase each of the bolded values by +1). If all these bolded values are different then check the candidate's original constraints in (b) to see if consistent with equations seen earlier

Question Number				S	cheme				Marks
	Stage	State	Action	Dest		Va	lue		
	May	3	1	0	75 + 1	50	= 225	*	
	(4)	2	2	0	50 + 1	50	= 200	)*	
		1	3	0	25 + 1		= 175	*	
		0	4	0	1	50 + 400	= 550	)*	
	April	3	3	0	75 + 1	50+ + 5	50 = 775	*	
	(6)		4	1		50 + 400 + 1			
			5	2	75 + 1	50 + 400 + 2			M1 A1 A1
		2	4	0		50 + 400 + 5			(April)
			5	1	50 + 1	50 + 400 + 1			
		1	5	0	25 + 1	50 + 400 + 5	50 = 112	5*	
	March	3	3	1	75 + 1		125 = 135		
	(5)		4	2		50 + 400 + 7			
			5	3	75 + 1	50 + 400 + 7			M1 A1ft A1 (March)
		2	4	1		50 + 400 + 1		-	(Watch)
			5	2	50 + 1	50 + 400 + 7	75 = 137	5*	
7. (a)		1	5	1	25 + 1	50 + 400 + 1	125 = 170	0*	
	Feb	3	0	1	75		700 = 1773		
	(2)		1	2	75 + 1		375 = 160		
			2	3	75 + 1		350 = 157		
		2	1	1	50 + 1		700 = 190		
			2	2	50 + 1		$\frac{375}{250} = 157$		
			3	3	50 + 1		350 = 155		M1 A1ft A1
		1	2	1	25 + 1		$\frac{700}{255} = 187$		(February)
			3	2	25 + 1		$\frac{375}{250} = 155$		(i cordary)
		0	4	3		50 + 400 + 1			
		0	3	1			700 = 1850		
			4 5	$\frac{2}{3}$		$\frac{50 + 400 + 11}{50 + 400 + 11}$			
	T	0							
	Jan (2)	0	23	0		$\frac{50 + 18}{50 + 13}$			
	(2)		4	2		$\frac{50}{50+400+11}$			M1 A1
			5	3		$\frac{50+400+1}{50+400+1}$			(January)
		<u> </u>	5					5	
	Month		January	y Fe	bruary	March	April	May	B1
	Number	made	3		3	5	5	3	
	Minimum	n cost: (£)	1700						B1 ( <b>13</b>
( <b>b</b> )	700×19-	-(6050+	their 1700)	= (£) 55:	50				M1 A1 (2 15 marks

Question Number	Scheme	Marks
	Notes for Question 7	
(April) if rows. Co 'ingred example : either th	arks – must bring optimal result from previous stage into calculations so for th none of 225, 200, 175 or 550 (the optimal results from May) are used then M0. ndone and credit rows that have been crossed out if they can still be read. Mu ients' (storage costs, overhead costs, additional worker cost) at least once per s for the six rows in April we must see at least one of these rows having a calcula ree or four values). Must have values in two of the three colums (State, Action and seen then the number stated in the Value column must be correct to imply t method has been used	Ignore extra st have right tage (as an tion that has , Dest). If no
above) a1A1: Any	at stage (April) completed. At least 6 rows, 'something' in each cell (but see M mark two states correct (condone extra rows) D for first stage. No extra rows	k guidance
a2M1: Sec above)	ond stage (March) completed. At least 6 rows, something in each cell (see M mark	guidance
,	ny two states correct – ft their * values/their smallest value from previous stage (cor	ndone extra
,	D for second stage. No extra rows	
a3M1: Thi above)	rd stage (February) completed. At least 12 rows, something in each cell (see M mar	k guidance
a5A1ft: Ar rows)	ny two states correct – ft their * values/their smallest value from previous stage (cor O for third stage. No extra rows	ndone extra
a4M1: Fou	rth stage completed. At least 4 rows, something in each cell (see M mark guidance D (no ft) for fourth stage. No extra rows	above)
	<ul> <li>but must have scored all previous M marks</li> <li>condone lack of units - but must have scored all previous M marks</li> </ul>	
b1M1:700 marks in (	$\times 19 - (5 \times 450 + 19 \times 200 + \text{their } 1700)$ or $7250 - \text{their } 1700$ . Must have scored at I	east two M
	O (condone lack of units) – correct answer with no working can score both marks in endent on at least two M marks awarded in (a))	n this part ( <b>but</b>

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